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I kurs. GEOMETRIYA

10-Mavzu: UCHBURCHAKLARNI YECHISH

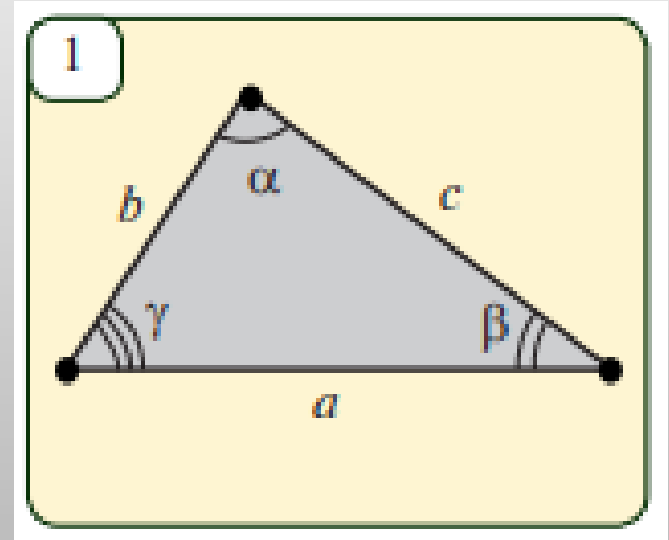



UCHBURCHAKLARNI YECHISH



Uchburchakning tomonlarini a , b , c bilan, bu tomonlar qarshisidagi burchaklarni mos ravishda α , β , γ bilan belgilaymiz (*1-rasm*). Uchburchakning tomonlari va burchaklarini bitta nom bilan — uning *elementlari* deb atashadi.

Uchburchakni aniqlovchi berilgan elementlariga ko‘ra, uning qolgan elementlarini topish *uchburchakni yechish deb yuritiladi*.



 **1-masala.** (Uchburchakni berilgan bir tomoni va unga yopishgan burchaklari bo'yicha yechish). Agar uchburchakda $a=6$, $\beta=60^\circ$ va $\gamma=45^\circ$ bo'lsa, uning uchinchi burchagi va qolgan ikki tomonini toping.

Yechish. 1. Uchburchak burchaklari yig'indisi 180° bo'lgani uchun

$$\alpha=180^\circ-\beta-\gamma=180^\circ-60^\circ-45^\circ=75^\circ.$$


Sinuslar teoremasidan foydalanib, qolgan ikki tomonni topamiz:

$$2. \frac{a}{\sin \alpha} = \frac{b}{\sin \beta} \quad \text{tenglikdan } b = a \cdot \frac{\sin \beta}{\sin \alpha} = 6 \cdot \frac{\sin 60^\circ}{\sin 75^\circ} \approx 6 \cdot \frac{0,8660}{0,9659} \approx 5,3794 \approx 5,4.$$

($\sin 60^\circ$ va $\sin 75^\circ$ qiymatlari mikrokalkulatorlarda topib qo'yildi, ularni darslikning 153-betidagi jadvaldan ham topishingiz mumkin).

$$3. \frac{a}{\sin \alpha} = \frac{c}{\sin \gamma} \quad \text{tenglikdan } c = a \cdot \frac{\sin \gamma}{\sin \alpha} = 6 \cdot \frac{\sin 45^\circ}{\sin 75^\circ} \approx 6 \cdot \frac{0,7071}{0,9659} \approx 4,3924 \approx 4,4.$$

Javob: $\alpha=75^\circ$; $\beta \approx 5,4$; $c \approx 4,4$.

 **2-masala.** (Uchburchakni berilgan ikki tomoni va ular orasidagi burchagi bo'yicha yechish). Agar uchburchakda $a = 6$, $b = 4$ va $\gamma = 120^\circ$ bo'lsa, uning uchinchi tomoni va qolgan burchaklarini toping.

Yechish. 1. Kosinuslar teoremasidan foydalanib, uchburchakning uchinchi c tomonini topamiz.

$$c = \sqrt{a^2 + b^2 - 2ab \cos \gamma} = \sqrt{36 + 16 - 2 \cdot 6 \cdot 4 \cdot (-0,5)} = \sqrt{76} \approx 8,7.$$

2. Endi, uchburchakning uchta tomonini bilgan holda, kosinuslar teoremasidan foydalanib, uchburchakning qolgan burchaklarini topamiz:

$$\cos \alpha = \frac{b^2 + c^2 - a^2}{2bc} = \frac{4^2 + 76 - 6^2}{2 \cdot 4 \cdot \sqrt{76}} \approx 0,8046.$$

$\cos \alpha \approx 0,8046$ tenglik asosida α burchakning qiymatini 153-betdagi jadvaldan aniqlaymiz (α — o'tkir burchak): $\alpha \approx 36^\circ$.

3. $\beta = 180^\circ - \alpha - \gamma \approx 180^\circ - (36^\circ + 120^\circ) = 24^\circ$.

Javob: $c \approx 8,7$; $\alpha \approx 36^\circ$, $\beta \approx 24^\circ$.



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TIAME

3-masala. (Uchburchakni berilgan uch tomoni bo'yicha yechish). Agar uchburchakda $a=10$, $b=6$ va $c=13$ bo'lsa, uning burchaklarini toping.

Yechish: 1. Uchburchak o'tmas burchakli bo'lishi yoki bo'lmasligini katta tomon qarshisidagi burchak kosinusining ishorasiga qarab aniqlaymiz:

$$\cos C = \frac{a^2 + b^2 - c^2}{2ab} = \frac{100 + 36 - 169}{2 \cdot 10 \cdot 6} = -\frac{33}{120} \approx -0,275 < 0.$$

Demak, C — o'tmas burchak ekan. Buni 153-betdagi jadvaldan C burchakning kattaligini aniqlashda hisobga olamiz. Jadvaldan kosinusi 0,275 ga teng burchak $\angle C_1 = 74^\circ$ ekanligini topamiz. Unda $\cos(180^\circ - \alpha) = -\cos \alpha$ formulaga ko'ra,

$$\angle C = 180^\circ - \angle C_1 = 180^\circ - 74^\circ = 106^\circ.$$

2. Sinuslar teoremasiga ko'ra,

$$\frac{a}{\sin A} = \frac{c}{\sin C}. \text{ Bundan, } \sin A = \frac{a \cdot \sin C}{c} = \frac{10 \cdot \sin 106^\circ}{13} = \frac{10 \cdot \sin 74^\circ}{13} \approx \frac{10 \cdot 0,9615}{13} \approx 0,7396.$$

A — o'tkir burchak bo'lgani uchun 153-betdagi jadvaldan $\angle A \approx 47^\circ$ ekanligini aniqlaymiz.

3. $\angle B \approx 180^\circ - (106^\circ + 47^\circ) = 26^\circ$.

Javob: $\angle A \approx 47^\circ$, $\angle B \approx 26^\circ$, $\angle C \approx 106^\circ$.